

5.2H Solve Quadratic Equations Using Square Roots to Find Real or Complex Solutions

#1 – 6: Simplify the following radicals.

1. $\sqrt{-9}$
 $3i$

2. $7\sqrt{-50}$
 $7\sqrt{-1 \cdot 25 \cdot 2}$
 $7 \cdot 5\sqrt{2}$
 $35i\sqrt{2}$

3. $2\sqrt{-3}$
 $2i\sqrt{3}$

4. $3\sqrt{-100}$
 $30i$

5. $11\sqrt{-18}$
 $11\sqrt{-1 \cdot 9 \cdot 2}$
 $33i\sqrt{2}$

6. $\sqrt{-121}$
 $11i$

7. What is the value of i^2 ?
 -1

#8 – 13: Simplify the following complex expressions.

8. $(3i)^2$
 $9i^2$
 -9

9. $(-5i)^2$
 $25i^2$
 -25

10. $(-i)^2$
 $i^2 =$
 -1

11. $(3-5i)^2$
 $9-30i+25i^2$
 $9-30i-25$
 $-16-30i$

12. $2(3+4i)^2$
 $2(9+24i+16i^2)$
 $2(-7+24i)$
 $-14+48i$

13. $(-2-7i)^2+5$
 $4+28i+49i^2+5$
 $4+28i-49+5$
 $-40+28i$

#14 – 17: Verify that each of the following values are solutions to the given equation. Show all of your work.

14. $-2x^2+3=21$; $x=3i, x=-3i$

$-2(3i)^2+3=21$
 $-2(9i^2)$
 $-2(9)(-1)$
 $18+3=21 \checkmark$

$-2(-3i)^2+3=21$
 $-2(9i^2)$
 $-18i^2$
 $18+3=21 \checkmark$

15. $(x-5)^2-1=-17$; $x=5+4i, x=5-4i$

$((5+4i)-5)^2-1=-17$
 $(4i)^2$
 $16i^2$
 $-16-1=-17 \checkmark$

$((5-4i)-5)^2-1=-17$
 $(-4i)^2-1$
 $16i^2-1$
 $-16-1=-17 \checkmark$

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#14 – 17 (continued): Verify that each of the following values are solutions to the given equation. Show all of your work.

16. $x^2 + 11 = 7$; $x = 2i$, $x = -2i$

$$(2i)^2 + 11 = 7$$

$$4i^2 + 11$$

$$4(-1) + 11 = 7 \checkmark$$

$$(-2i)^2 + 11 = 7$$

$$4i^2$$

$$-4 + 11 = 7 \checkmark$$

17. $(x+2)^2 = -25$; $x = -2+5i$, $x = -2-5i$

$$((-2+5i)+2)^2 = -25$$

$$(5i)^2$$

$$25i^2$$

$$25(-1) = -25 \checkmark$$

$$((-2-5i)+2)^2 = -25$$

$$(-5i)^2$$

$$25i^2$$

$$25(-1) = -25 \checkmark$$

#18 – 21: Solve each equation for real or complex solutions. Verify your solutions.

18. $x^2 + 3 = 51$

$$\sqrt{x^2} = \sqrt{48}$$

$$|x| = \sqrt{16 \cdot 3}$$

$$x = \pm 4\sqrt{3}$$

19. $\sqrt{(x-1)^2} = \sqrt{-24}$

$$|x-1| = \sqrt{-1 \cdot 4 \cdot 6}$$

$$x-1 = \pm 2i\sqrt{6}$$

$$+1 \quad +1$$

$$x = 1 + 2i\sqrt{6}, x = 1 - 2i\sqrt{6}$$

✓ Verify your solution(s):

$$(4\sqrt{3})^2 + 3 = 51$$

$$16 \cdot 3 + 3 = 51 \checkmark$$

$$(-4\sqrt{3})^2 + 3$$

$$16 \cdot 3 + 3 = 51 \checkmark$$

✓ Verify your solution(s):

$$((1 + 2i\sqrt{6}) - 1)^2 = -24$$

$$(2i\sqrt{6})^2$$

$$4i^2 \cdot 6$$

$$24(-1) = -24 \checkmark$$

$$((1 - 2i\sqrt{6}) - 1)^2 = -24$$

$$(-2i\sqrt{6})^2$$

$$4i^2 \cdot 6$$

$$24(-1) = -24 \checkmark$$

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#18 – 21 (continued): Solve each equation for real or complex solutions. Verify your solutions.

20. $3x^2 - 27 = 0$

$$\begin{aligned} 3x^2 &= 27 \\ \sqrt{x^2} &= \sqrt{9} \\ |x| &= 3 \\ \boxed{x = 3 \text{ or } x = -3} \end{aligned}$$

✓ Verify your solution(s):

$$\begin{aligned} 3(3)^2 - 27 &= 0 \\ 3 \cdot 9 - 27 &= 0 \checkmark \\ 3(-3)^2 - 27 &= 0 \\ 3 \cdot 9 - 27 &= 0 \checkmark \end{aligned}$$

21. $5(x+1)^2 - 3 = -48$

$$\begin{aligned} 5(x+1)^2 &= -45 \\ \sqrt{(x+1)^2} &= \sqrt{-9} \\ |x+1| &= 3i \\ x+1 &= \pm 3i \\ \boxed{x = -1 + 3i, x = -1 - 3i} \end{aligned}$$

✓ Verify your solution(s):

$$\begin{aligned} 5((-1+3i)+1)^2 - 3 &= -48 & 5((-1-3i)+1)^2 - 3 &= -48 \\ 5(3i)^2 & & 5(-3i)^2 & \\ 5 \cdot 9i^2 & & 5 \cdot 9i^2 & \\ 45i^2 & & 45i^2 & \\ -45 - 3 &= -48 \checkmark & -45 - 3 &= -48 \checkmark \end{aligned}$$

22. The height, h , of a water balloon (in feet) at time t (in seconds) is given by the equation

$h(t) = -16(t - 0.45)^2 + 32$. If a student throws the balloon and it lands on the ground, how long is the balloon in the air? Verify your solution(s).

$$\begin{aligned} 0 &= -16(t - 0.45)^2 + 32 \\ -32 &= -16(t - 0.45)^2 \\ \sqrt{2} &= \sqrt{(t - 0.45)^2} \\ \pm \sqrt{2} &= |t - 0.45| \\ * \boxed{t = 0.45 + \sqrt{2}} & \quad t = 0.45 - \sqrt{2} \approx -0.96 \text{ (extraneous)} \\ \#23 - 26: \text{ Find the real and/or complex roots of each function. Verify your solutions!} & \end{aligned}$$

23. $f(x) = x^2 - 125$

$$\begin{aligned} x^2 - 125 &= 0 \\ \sqrt{x^2} &= \sqrt{125} \\ |x| &= \sqrt{125} = 5\sqrt{5} \\ \boxed{x = 5\sqrt{5} \text{ or } x = -5\sqrt{5}} \end{aligned}$$

✓ Verify your solution(s):

$$\begin{aligned} (5\sqrt{5})^2 - 125 &= 0 & (-5\sqrt{5})^2 - 125 &= 0 \\ 25 \cdot 5 - 125 &= 0 \checkmark & 25 \cdot 5 - 125 &= 0 \checkmark \end{aligned}$$

24. $f(x) = (x+7)^2$

$$\begin{aligned} \sqrt{(x+7)^2} &= \sqrt{0} \\ |x+7| &= 0 \\ x+7 &= 0 \\ \boxed{x = -7} \end{aligned}$$

✓ Verify your solution(s):

$$\begin{aligned} (-7+7)^2 &= 0 \\ 0^2 &= 0 \checkmark \end{aligned}$$

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#23 – 26 (continued): Find the real and/or complex roots of each function. Verify your solutions!

25. $f(x) = -2(x-2)^2 - 18$

$$\begin{aligned} -2(x-2)^2 - 18 &= 0 \\ -2(x-2)^2 &= 18 \\ \sqrt{(x-2)^2} &= \sqrt{-9} \\ |x-2| &= 3i \\ x-2 &= \pm 3i \\ x &= 2+3i, x=2-3i \end{aligned}$$

✓ Verify your solution(s):

$$\begin{aligned} -2(2+3i-2)^2 - 18 &= 0 & -2(2-3i-2)^2 - 18 &= 0 \\ -2(3i)^2 & & -2(-3i)^2 & \\ 9i^2 & & 9i^2 & \\ -2(-9) - 18 &= 0 \checkmark & -2(-9) - 18 &= 0 \checkmark \end{aligned}$$

26. $f(x) = 4x^2 + 24$

$$\begin{aligned} 4x^2 + 24 &= 0 \\ 4x^2 &= -24 \\ \sqrt{x^2} &= \sqrt{-6} \\ |x| &= i\sqrt{6} \\ x &= i\sqrt{6} \text{ or } -i\sqrt{6} \end{aligned}$$

✓ Verify your solution(s):

$$\begin{aligned} 4(i\sqrt{6})^2 + 24 &= 0 & 4(-i\sqrt{6})^2 + 24 &= 0 \\ 4 \cdot i^2 \cdot 6 & & 4(i^2 \cdot 6) & \\ -24 + 24 &= 0 \checkmark & -24 + 24 &= 0 \checkmark \end{aligned}$$

27. The area of a square can be found using the formula $A = s^2$, where “A” is the area and “s” is the length of one side. If the area of a square is 50 square inches, what is the length of one side? Round your answer to the nearest thousandth and verify your solution(s).

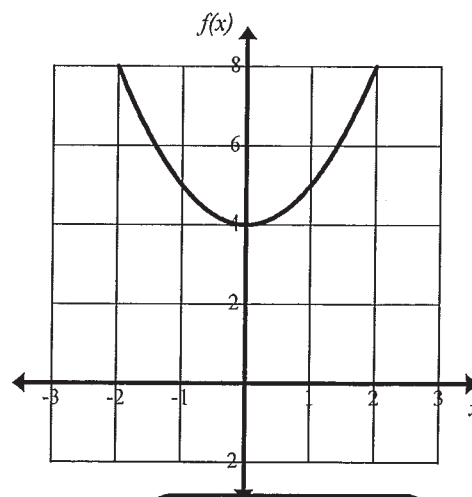
$$\begin{aligned} A &= s^2 \\ \sqrt{50} &= \sqrt{s^2} \\ \sqrt{25 \cdot 2} &= |s| \\ \pm 5\sqrt{2} &= s \\ \text{But length is positive} & \\ s &\approx 7.071 \text{ in} \end{aligned}$$

$$\begin{aligned} (7.071)^2 &= 50 \\ 49.999 &\approx 50 \checkmark \end{aligned}$$

28. The function $f(x) = x^2 + 4$ has no x -intercepts, as shown in the graph to the right. Use algebra to show that no real roots exist for this function.

$$\begin{aligned} x^2 + 4 &= 0 \\ \sqrt{x^2} &= \sqrt{-4} \\ |x| &= 2i \end{aligned}$$

$$\begin{aligned} x &= 2i \text{ or } x = -2i \\ \text{Both roots are imaginary} \end{aligned}$$



Section 5.2H